

Greenhouse effect: the relative contributions of emission height and total absorption

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ABSTRACT

Since the 1970's, results from radiative transfer models unambiguously show that an increase in the CO₂ concentration leads to an increase of the greenhouse effect. However, this robust result is often misunderstood and often questioned. A common argument is that the CO₂ greenhouse effect is saturated (i.e. does not increase) as CO₂ absorption of an entire atmospheric column, named absorptivity, is saturated. This argument is erroneous firstly because absorptivity by CO₂ is currently not fully saturated and still increases with CO₂ concentration, and secondly because a change in emission height explains why the greenhouse effect may increase even if the absorptivity is saturated. However, these explanations are only qualitative. In this article, we first propose a way of quantifying the effects of both the emission height and absorptivity and we illustrate which one of the two dominates for a suite of simple idealized atmospheres. Then, using a line by line model and a representative standard atmospheric profile, we show that the increase of the greenhouse effect due to an increase of CO₂ from its current value is primarily due (about 90%) to the change in emission height. For an increase of water vapor, the change in absorptivity plays a more important role (about 40%) but the change in emission height still has the largest contribution (about 60%).

1. Introduction

To establish the physical laws that govern the surface temperature of a planet, Fourier (1824; 1837) made the analogy between a vessel covered with plates of glass and the Earth surface covered by the atmosphere (Pierrehumbert, 2004). Using this framework, Arrhenius (1896) made the first estimate of the greenhouse effect and of the sensitivity of the surface temperature to a change in CO₂ concentration of the atmosphere. His computation was based on a single layer model where the surface was covered by an isothermal atmosphere for which the outgoing long-

wave flux at the top-of-the-atmosphere (TOA) reads:

$$\bar{F} = \tilde{\mathcal{T}}_s \bar{B}(T_s) + (1 - \tilde{\mathcal{T}}_s) \bar{B}(T_a) \quad (1)$$

where $\bar{B}(T)$ is the black body emission, i.e. the Stefan-Boltzmann law, for a temperature T , $\tilde{\mathcal{T}}_s$ is the total broadband hemispherical transmissivity, i.e. the transmissivity for radiation crossing the whole atmosphere, from its top to the surface, averaged over the longwave domain (overline variables refer to variables averaged over the longwave domain) and over an hemisphere. As we assume scattering in the longwave domain is negligible, the broadband absorptivity of the atmosphere in the longwave domain is equal to $1 - \tilde{\mathcal{T}}_s$ and is equal to the broadband emissivity of the atmosphere. T_s is the surface temperatures and T_a a bulk temperature of the atmosphere, generally called emission temperature. The broadband greenhouse effect, de-

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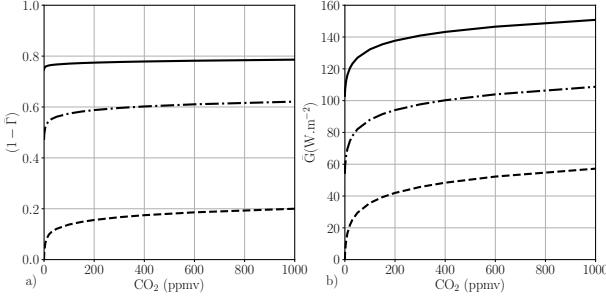


FIG. 1. **a)** Broadband absorptivity $(1 - \bar{\mathcal{T}}_s)$ of the atmosphere and **b)** broadband greenhouse effect \bar{G} at the tropopause as a function of the CO₂ concentration for the standard MLS atmospheric profile (McClatchey et al., 1972; Anderson et al., 1986) (continuous line), for the same profile where the water amount has been divided by 10 (dash-dot line) or set to zero (no water vapor, dash line). H₂O and CO₂ are the only two absorbing gases considered. The computations have been done with the 4A line-by-line model (Scott and Chedin, 1981; Cheruy et al., 1995). The broadband absorptivity is the average monochromatic absorptivity weighted by the Planck function at the surface temperature. The greenhouse effect at the tropopause is the difference between the flux emitted by the surface and the net flux at the tropopause (200 hPa).

fined as $\bar{G} = \bar{B}(T_s) - \bar{F}$, reads with this model:

$$\bar{G} = (1 - \bar{\mathcal{T}}_s)(\bar{B}(T_s) - \bar{B}(T_a)) \quad (2)$$

Although this equation has important limitations, it shows that the greenhouse effect is the product of two terms. The first is an optical characteristic, namely the absorptivity of the atmosphere $(1 - \bar{\mathcal{T}}_s)$. The larger the absorptivity, the larger the greenhouse effect. The second is an energy term that depends on thermodynamic variables, the surface temperature and the emission temperature of the atmosphere. The larger the difference between the two temperatures, the larger the greenhouse effect.

The broadband absorptivity of the atmosphere increases when the amount of water vapor increases, which supports the simple idea that an increase of atmospheric absorptivity in the infrared increases the greenhouse effect. However, the broadband absorptivity shows very little increase when the CO₂ concentration increases, especially for regular amounts of water vapor (Fig. 1-a). This is the well known “saturation effect” of CO₂ absorption (Archer, 2011; Pierrehumbert, 2011; Zhong and Haigh, 2013), first pointed out by Ångström (1900) who questioned the results of Arrhenius (1896) showing the impact of CO₂ concentration on the Earth surface temperature. It has been shown that the CO₂ absorption is not fully saturated (Pierrehumbert, 2011; Shine et al., 1995), and that a CO₂ increase modifies both the broadband and the spectral flux at the TOA (Kiehl, 1983; Charlock, 1984; Harries et al., 2001; Mlynczak et al., 2016). This “saturation” argument is still used in the public debate to claim that an increase of CO₂ concentration has very limited impact, if any, on the greenhouse effect.

The “saturation paradox” can be summarized as follows: why does the greenhouse effect increase with the CO₂ concentration (Fig. 1-b) whereas the broadband absorptivity does not increase as much, especially when water vapor is present (Fig. 1-a)? As highlighted by Eq. 2, the absorptivity is not the only main parameter that controls the greenhouse effect; the emission temperature T_a of the atmosphere is also fundamental. If the increase of CO₂ concentration has little impact on absorptivity, it has a significant impact on T_a . When the CO₂ increases, the infrared radiation that escapes toward space is emitted by the atmosphere at a higher altitude. As most of the radiation is emitted by the troposphere, higher altitude means lower emission temperature, lower value of the Planck function, lower value of the radiation emitted toward space and therefore higher value of the greenhouse effect (Hansen et al., 1981; Pierrehumbert, 2010; Archer, 2011; Benestad, 2017). For a doubling of the CO₂ concentration, the average value of the change in emission height is about 150 m, assuming that the radiative forcing of about $\approx 4 \text{ W m}^{-2}$ can be translated into a change in black body temperature emission, and then into a change in emission height assuming a temperature vertical gradient of $\approx 6.5 \text{ K/km}$ (Held and Soden, 2000).

Beyond the single layer model, for fundamental physical reasons, the increase of the greenhouse effect due to an increase of the concentration of an absorbing gas, in particular CO₂, is partly due to an increase of absorptivity and partly due to an increase of emission height (Pierrehumbert, 2010). However, the contribution of each of these two effects has not been quantified yet, and the main goals of this paper are to present a framework that allows quantifying the contribution of these two effects, and to perform the quantification. A second goal is to quantify the change in emission height, and not only its impact on the flux at the TOA. This offers the possibility to propose a new quantitative simplified description of the greenhouse effect that is more realistic than the too simple single layer model called blanket model (Benestad, 2017).

In this study, we will use only prescribed atmospheric profiles and will therefore compute the forcing when changing the absorbing gas concentration. All calculations are for cloudless skies. In section 2 we present the framework that allows to separate and quantify the contribution of absorptivity and that of emission height to the flux at the tropopause, and therefore to the greenhouse effect. To allow some analytical developments, especially for simple limiting cases, we consider monochromatic radiances and idealized vertical atmospheric profiles. In section 3 we still consider radiances but with realistic atmospheric profiles. This will help us to interpret the results presented in section 4, where we compute the flux at the tropopause over the whole thermal infrared domain and where we independently increase the concentration of the two most important greenhouse gases on Earth, H₂O and

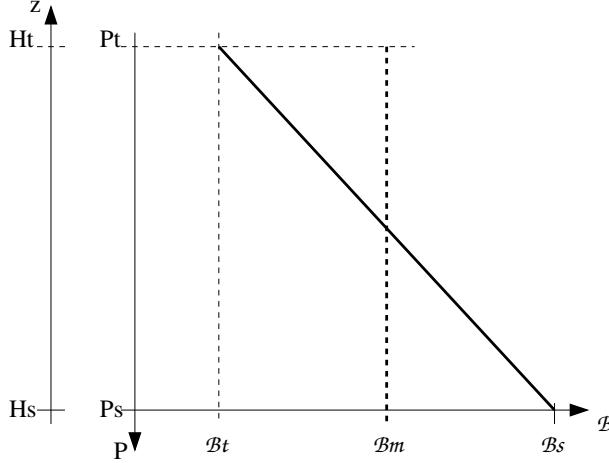


FIG. 2. Vertical profile of the Planck function \mathcal{B} for an isothermal atmosphere (bold dashed line at \mathcal{B}_m) and for an idealized temperature profile for which the Planck function increases linearly with pressure P from \mathcal{B}_t at the tropopause (pressure P_t and altitude H_t) to \mathcal{B}_s at the surface (pressure P_s and altitude H_s) (bold continue line). The pressure axis has a linear scale whereas the altitude axis has a logarithmic scale.

CO_2 . The temperature adjustment of the stratosphere is also analyzed. Finally, summary and conclusion are given in section 5.

2. Formulation with simplified conditions

To present the main concepts and to facilitate some analytical developments, we first consider the very simple case of an idealized atmosphere where the monochromatic absorption coefficient is constant along the vertical and the volumetric mass density only depends on pressure and therefore on altitude z

$$\rho(z) = \rho(0)e^{-z/h_r} \quad (3)$$

where h_r is the scale height ($h_r \approx 8\text{km}$ on Earth). Hydrostatic pressure follows a law of the same type as density: $P(z) = P(0)e^{-z/h_r}$. To quantify the radiative forcing of CO_2 , it has been shown that the change of the net flux at the tropopause is much more relevant than the change of the net flux at the top of the atmosphere (Shine et al., 1995; Hansen et al., 1997; Stuber et al., 2001). To keep the atmospheric profile as simple as possible, we ignore the stratosphere in a first step and then show Sect. 4-d that this simplification has little impact for the key points addressed in this study. We therefore consider the troposphere only, i.e. an atmosphere, which vertical extent ends at the tropopause. A last simplification is to assume that the temperature vertical profile is such that the monochromatic radiance emitted by a black body (or Planck function) $\mathcal{B}(P)$ increases linearly with pressure P (Fig. 2):

$$\mathcal{B}(P) = \mathcal{B}(P_s) + \frac{P - P_s}{P_t - P_s}(\mathcal{B}(P_t) - \mathcal{B}(P_s)) \quad (4)$$

where $P_s = 1000\text{hPa}$ and $P_t = 200\text{hPa}$ are the pressure at the surface and at the tropopause, $H_s = 0$ and $H_t = h_r \log(P_s/P_t) \approx 12.9\text{km}$ are the altitude of the surface and the tropopause, respectively. Note that curly letters refer to monochromatic directional variables. We consider two contrasted profiles (Fig. 2): a profile where \mathcal{B} decreases from the Planck function at surface \mathcal{B}_s to a value \mathcal{B}_t at the tropopause ($\mathcal{B}(P_s) = \mathcal{B}_s$ and $\mathcal{B}(P_t) = \mathcal{B}_t$), and an isothermal profile chosen so that the two profiles have the same mass weighted mean value: $\mathcal{B}(P_s) = \mathcal{B}(P_t) = \mathcal{B}_m = 0.5(\mathcal{B}_t + \mathcal{B}_s)$. The Planck function is computed for a wave number $v_c = 550\text{cm}^{-1}$ (corresponding to a wavelength $\lambda_c \approx 18\mu\text{m}$) close to the strong $\text{CO}_2 15\mu\text{m}$ absorption band and for temperatures $T_s = 294\text{K}$ ($\mathcal{B}_s \approx 0.144\text{Wm}^{-2}\text{sr}^{-1}$) and $T_t = 220\text{K}$ ($\mathcal{B}_t \approx 0.056\text{Wm}^{-2}\text{sr}^{-1}$). We assume the atmosphere has an homogeneous concentration of absorbing gases and we neglect the effects of pressure and temperature on the specific absorption coefficient k (in m^2kg^{-1}). Therefore k is constant along the vertical. The surface is assumed to be a perfect black body. We also assume that radiation propagates only along the vertical, which allows to replace the integral on the zenith angle by considering one single angle. The radiative exchanges are computed at a given frequency and with a formalism adapted for general plane parallel atmospheres (Schwarzkopf and Fels, 1991).

a. Basic equations and the limiting case of the single layer model

With the above assumptions, the expression of the optical thickness between the tropopause and a layer of pressure P at altitude z simplifies as

$$\tau(P) = kf(P - P_t)/g \quad (5)$$

where g is the gravity in ms^{-2} . We introduce f , which is a multiplicative factor to allow a proportional change in absorption within the whole atmosphere. By default, $f = 1$. The spectral outgoing radiance \mathcal{F} at the tropopause in the zenith direction then reads (Pierrehumbert, 2010):

$$\begin{aligned} \mathcal{F} &= \mathcal{T}_s \mathcal{B}_s + \int_{P_t}^{P_s} \frac{\partial \mathcal{T}(P)}{\partial P} \mathcal{B}(P) dP \\ &= \mathcal{F}_s + \mathcal{F}_a \end{aligned} \quad (6)$$

where $\mathcal{T}(P)$ is the directional transmissivity between altitude of pressure P and the tropopause

$$\mathcal{T}(P) = e^{-\tau(P)}, \quad (7)$$

$\mathcal{T}_s = \mathcal{T}(P_s) = e^{-\tau_s}$ is the transmissivity of the troposphere with $\tau_s = \tau(P_s)$ the total optical thickness of the troposphere, i.e. from the tropopause to the surface. $\mathcal{F}_s = \mathcal{T}_s \mathcal{B}_s$ is the radiance that is emitted by the surface and that

reaches the tropopause. \mathcal{F}_a is the vertical integral of the radiance that is emitted by the troposphere and that reaches the tropopause.

Equation 6 may be written as:

$$\mathcal{F} = \mathcal{T}_s \mathcal{B}_s + (1 - \mathcal{T}_s) \mathcal{B}_e \quad (8a)$$

where \mathcal{B}_e is the equivalent blackbody emission of the atmosphere:

$$\mathcal{B}_e = \int_{P_t}^{P_s} \mathcal{B}(P) \omega(P) dP \quad (8b)$$

and

$$\omega(P) = \frac{1}{1 - \mathcal{T}_s} \frac{\partial \mathcal{T}(P)}{\partial P}. \quad (8c)$$

Equation 8a has the same form as the classical single layer model (Eq. 1) except that here it is spectrally resolved. This equation makes explicit that the radiance at the tropopause depends directly on the transmissivity \mathcal{T}_s , and therefore on the total optical thickness τ_s of the troposphere. This transmissivity \mathcal{T}_s impacts both the radiance that reaches the tropopause emitted by the surface and the radiance that reaches the tropopause emitted by the troposphere.

The equivalent blackbody emission \mathcal{B}_e of the atmosphere is the mean value of the blackbody emission $\mathcal{B}(P)$ weighted by the $\omega(P)$ function (Eq. 8b). For optically very thin atmospheres ($\tau_s \ll 1$), \mathcal{B}_e is equal to the pressure-weighted mean of $\mathcal{B}(P)$. Then $\mathcal{B}_e \approx [\mathcal{B}(P_t) + \mathcal{B}(P_s)]/2$ and is the same for the two idealized atmospheric profiles considered in this section (Appendix Sect. A1).

When the troposphere is optically thin, the radiance \mathcal{F} at the tropopause decreases when the optical thickness τ_s of the troposphere increases, starting from a value $\mathcal{F} = \mathcal{B}_s$ when $\tau_s = 0$ (Fig. 3, black line). As long as $\tau_s \ll 1$, the decrease of the radiance \mathcal{F} at the tropopause is proportional to τ_s and similar for both atmospheric profiles because the pressure-weighted mean temperature of both tropospheres is the same (see Sect. A1-a in Appendix). When the troposphere is isothermal, this decrease gradually slows down from optical thickness τ_s larger than 0.5 and reaches a plateau when the optical thickness is larger than about 4. When the troposphere is non isothermal, the slowdown is not as fast as for the isothermal case and the decrease continues for optical thickness larger than 4. The limiting value of the radiance at the tropopause for infinite value of the optical thickness is much smaller (and therefore the greenhouse effect much higher) in the non-isothermal case compared to the isothermal case.

The model generally used in simplified explanations of the greenhouse effect (Eq. 1) assumes that the troposphere is isothermal along the vertical. With this assumption, the flux at the tropopause does not decrease any more when the total optical thickness τ_s increases if τ_s is larger than 4. It is then said that the greenhouse effect “saturates”. This saturation effect almost disappears when the temperature

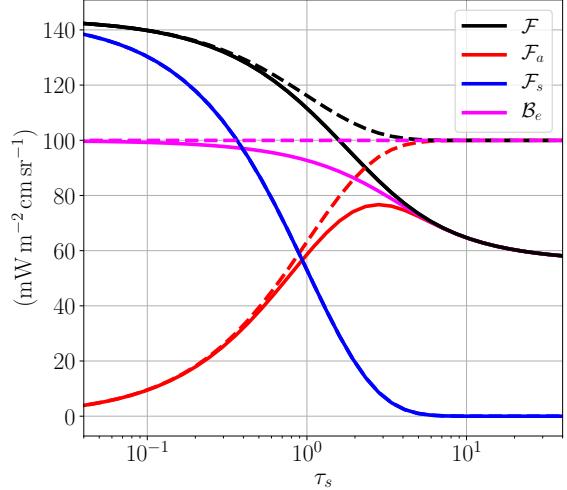


FIG. 3. Radiance at the tropopause (black: total, \mathcal{F} ; blue: emitted by the surface, \mathcal{F}_s ; red: emitted by the troposphere, \mathcal{F}_a , Eq. 6), weighted average black body emission of the troposphere (magenta, \mathcal{B}_e , Eq. 8b), as a function of the total optical thickness τ_s of the troposphere for an isothermal vertical profile (dashed line) and a profile where the temperature decreases with altitude (continuous line). The idealized troposphere is 12.6 km high with uniform absorption coefficient and volumetric mass density that only depends on pressure (see Sect. 2-a).

decreases with height: The greenhouse effect continues to increase when the optical thickness τ_s increases, even for large value of τ_s . For a non-isothermal troposphere the altitude where the emitted radiation escapes to space matters. We now present how this effect of emission height can be quantified.

b. Contribution of absorptivity and emission height to radiance changes

The sensitivity of the radiance \mathcal{F} at the tropopause to a fractional change in amount of absorbing gases reads, according to Eq. 8:

$$\frac{\partial \mathcal{F}}{\partial f} \equiv \mathcal{F}' = \frac{\partial \mathcal{T}_s}{\partial f} (\mathcal{B}_s - \mathcal{B}_e) + (1 - \mathcal{T}_s) \frac{\partial \mathcal{B}_e}{\partial f} \quad (9)$$

which we rewrite as:

$$\mathcal{F}' = \mathcal{F}'_{\mathcal{T}} + \mathcal{F}'_{Z_e} \quad (10a)$$

$$\mathcal{F}'_{\mathcal{T}} = \frac{\partial \mathcal{T}_s}{\partial f} (\mathcal{B}_s - \mathcal{B}_e) \quad (10b)$$

$$\mathcal{F}'_{Z_e} = (1 - \mathcal{T}_s) \frac{\partial \mathcal{B}_e}{\partial f} \quad (10c)$$

These three terms are shown in Fig. 4 as a function of the total optical thickness τ_s of the troposphere.

According to Eq. 10b, $\mathcal{F}'_{\mathcal{T}}$ quantifies how much the radiance \mathcal{F} at the tropopause is directly impacted by a change

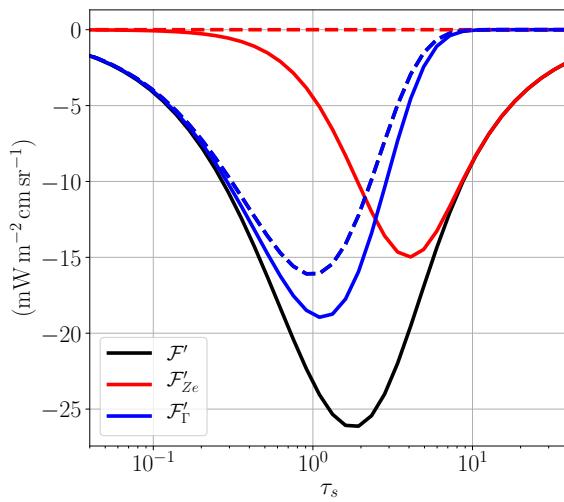


FIG. 4. Sensitivity \mathcal{F}' of the radiance at the tropopause to a fractional change in absorbing gas concentration as a function of the total optical thickness τ_s of the troposphere. Results are shown for the same isothermal (dashed line) and idealized decreasing temperature (continuous line) profiles as in Fig. 3. The sensitivity \mathcal{F}' (black) is decomposed in a contribution due to change in absorptivity (\mathcal{F}'_T , blue line) and a contribution due to change in emission height (\mathcal{F}'_{Z_e} , red line). For the isothermal profile, \mathcal{F}' is not visible as it is covered by \mathcal{F}'_T .

in the transmissivity \mathcal{T}_s , and therefore by a change in the absorptivity $\mathcal{A}_s = 1 - \mathcal{T}_s$, when the amount of absorbing gases changes. \mathcal{F}'_T is the sensitivity of the radiance at the tropopause if the troposphere is isothermal, or would be isothermal, at a temperature that corresponds to a black body emission \mathcal{B}_e (i.e. $\partial \mathcal{B}_e / \partial f = 0$). For both temperature profiles, the absolute value of \mathcal{F}'_T linearly increases with τ_s , is maximum for $\tau_s \approx 1$, becomes very small for τ_s larger than 4 and is almost zero when the troposphere is fully opaque (Fig. 4). \mathcal{F}'_T is slightly higher for the non-isothermal profile as \mathcal{B}_e has a smallest value with this profile compared to the isothermal profile (Fig. 3).

\mathcal{F}'_{Z_e} quantifies how much the radiance at the tropopause is impacted by a change in \mathcal{B}_e when the amount of absorbing gases changes. Radiance \mathcal{B}_e (Eq. 8b) is the weighted average of the Planck function over the whole troposphere with a weight $\omega(P)$ (Eq. 8c), which depends on the optical exchange factor between the atmosphere at pressure P and the tropopause (Dufresne et al., 2005). This weight varies from a function that is constant with pressure when the total optical thickness is low ($\tau_s \ll 1$) to a function that is maximum at the tropopause, decreases with increasing pressure and is almost zero close to the surface when the total optical thickness is large ($\tau_s \gg 1$) (Fig. 5, and Sect. A1-b in Appendix). As a consequence, the radiation that reaches the tropopause is emitted on average at lower pressure, i.e. at higher altitude, when the optical thickness of the troposphere increases. It is said that the “emis-

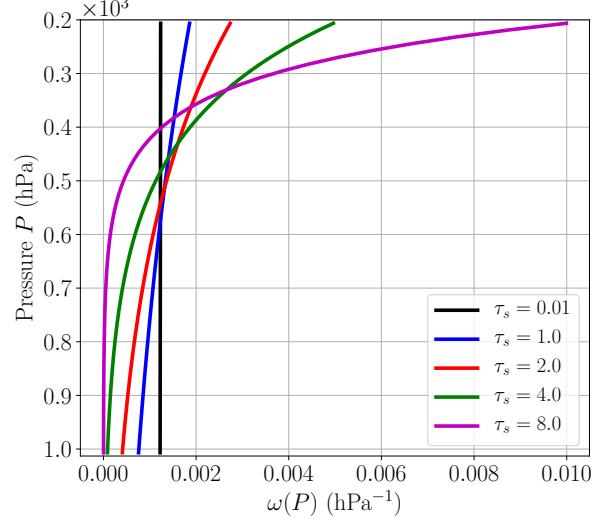


FIG. 5. Vertical profile of $\omega(P)$ for different values of the total optical thickness τ_s of the troposphere (black: 0.01, blue: 1, red: 2, green: 4, magenta: 8) for the same idealized troposphere with a uniform absorption coefficient as in Fig. 3. $\omega(P)$ is the normalized optical exchange factor between the troposphere at pressure P and the tropopause (Eq. 8c).

sion height” increases (Hansen et al., 1981; Held and Soden, 2000; Pierrehumbert, 2010; Archer, 2011; Benestad, 2017). The variable \mathcal{F}'_{Z_e} quantifies how much this change in emission height impacts the radiance at the tropopause. It is zero for an isothermal troposphere since $\frac{\partial \mathcal{B}_e}{\partial f} = 0$. If the temperature of the troposphere decreases with height, an increase of emission height yields a decrease of the temperature, a decrease of the Planck function and therefore a decrease of the upward radiance at the tropopause. The sensitivity \mathcal{F}'_{Z_e} due to change in emission height increases with the total optical thickness τ_s of the troposphere, reaches a maximum for $\tau_s \approx 4$, and then slowly decreases (red line on Fig. 4).

c. Emission height

After defining the contribution of the change in emission height to the change in radiance at the tropopause, we now define the emission height itself. Since we assume in this section that the absorption coefficient k is constant, the optical thickness increases linearly with pressure (Eq. 5). Therefore, many radiative variables are easier to compute and to interpret in pressure coordinate rather than in altitude coordinate. We will therefore continue to write the equations in pressure coordinate, and the “emission height” will be defined as the altitude corresponding to the “emission pressure”.

The relative contribution $\Omega(P)$ of a layer of thickness dP at pressure P to the radiance \mathcal{F}_a reads, according to Eq. 6:

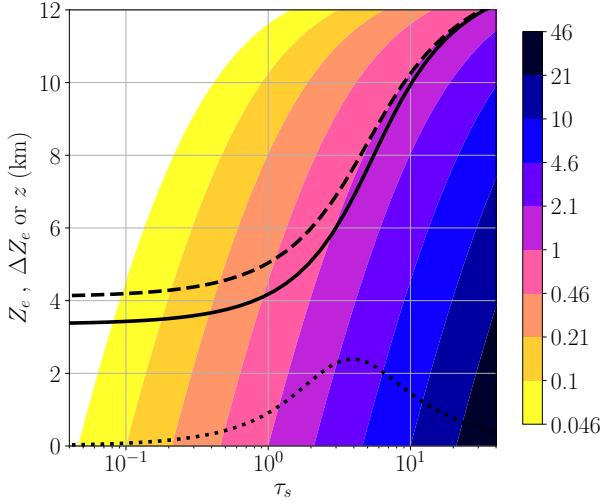


FIG. 6. Emission height Z_e (black line) as a function of the total optical thickness τ_s for a troposphere with an idealized decreasing temperature profile as in Fig. 3 (continuous line) and change ΔZ_e of this emission height when the amount of absorbing gas is doubled (dotted line). The dashed line displays the emission height Z_e for the isothermal profile. Shaded display the function $\tau(\tau_s, z)$ defined as the optical thickness τ at altitude z when the total optical thickness of the troposphere is τ_s . For instance the emission height Z_e almost coincides with the isoline $\tau(\tau_s, z) = 1$ for optically thick atmospheres ($\tau_s > 4$).

$$\Omega(P)dP = \frac{\frac{\partial \mathcal{T}(P)}{\partial P} \mathcal{B}(P)dP}{\int_{P_t}^{P_s} \frac{\partial \mathcal{T}(P)}{\partial P} \mathcal{B}(P)dP}. \quad (11)$$

Using (Eq. 8b and 8c), this equation may be written as:

$$\Omega(P) = \frac{1}{(1 - \mathcal{T}_s)\mathcal{B}_e} \frac{\partial \mathcal{T}(P)}{\partial P} \mathcal{B}(P) \quad (12)$$

$$= \omega(P) \frac{\mathcal{B}(P)}{\mathcal{B}_e}. \quad (13)$$

According to Eq. 8b, $\int_{P_t}^{P_s} \Omega(P)dP = 1$, $\Omega(P)$ is the probability density function that photons emitted by the troposphere and that reached the tropopause have been emitted at an altitude where the pressure is P . Therefore, the mean pressure where the photons reaching the tropopause have been emitted is:

$$P_e = \int_{P_t}^{P_s} P \Omega(P)dP. \quad (14)$$

This mean emission pressure P_e will be simply named “emission pressure”, and the “emission height” Z_e will be defined as the altitude where the pressure is equal to P_e . However, one should have in mind that the actual emission pressure and emission height are not single values but are functions, which are non-zero in a wide pressure and altitude range. In particular they span the whole troposphere when the optical thickness is small.

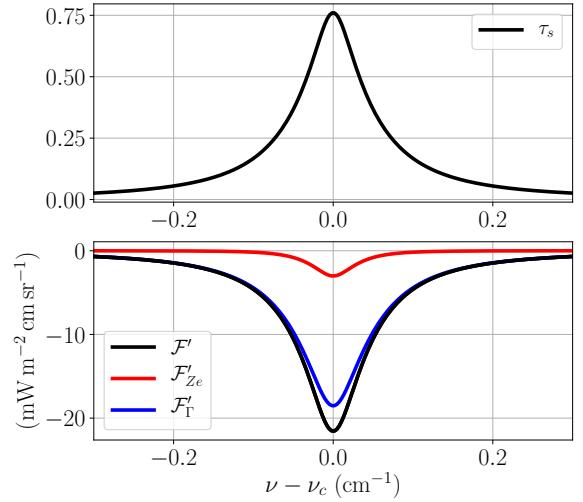


FIG. 7. Total optical thickness τ_s (top) and sensitivity of the radiance at the tropopause to a fractional change in absorbing gases (bottom) as a function of wave number ν for a single weak absorption line and the MLS atmospheric profile. This sensitivity (\mathcal{F}' , black line) is decomposed in the contribution due to the change in emission height (\mathcal{F}'_{Z_e} , red line) and due to the change in absorptivity (\mathcal{F}'_T , blue line). The abscissa is the distance from line center ($\nu_c = 550\text{cm}^{-1}$), the line width is 0.1cm^{-1} near the surface.

When the troposphere is isothermal, $\mathcal{B}(P) = \mathcal{B}_e$ and therefore $\Omega(P) = \omega(P)$. The probability density that a photon emitted by the troposphere and that reached the tropopause has been emitted at a level of pressure P is equal to the probability density that a photon going downward at the tropopause is absorbed at level of pressure P . This is consistent with the reciprocity principle. Therefore, when the total optical thickness τ_s is small, the emission pressure is equal to the average between the tropopause pressure and the pressure at surface, i.e. $(P_t + P_s)/2$. The corresponding altitude is slightly higher than 4km, which is consistent with what is observed in Fig. 6. Compared to the isothermal profile, Z_e is lower when the temperature decreases with height as the Planck function gives more weight to the lower and warmer part of the troposphere.

Starting from the altitude where the pressure is $(P_t + P_s)/2$, the emission height Z_e increases when the total optical thickness τ_s increases (Fig. 6). The emission height Z_e is commonly approximated as the altitude where the optical thickness is one (Pierrehumbert, 2010; Huang and Bani Shahabadi, 2014). For the profiles considered here, this approximation is valid as soon as the total optical thickness is larger than about 4 (Fig. 6).

3. Results with more realistic cloudless atmospheres

We now abandoned previous idealized verticale profil and consider a realistic cloudless atmosphere, namely

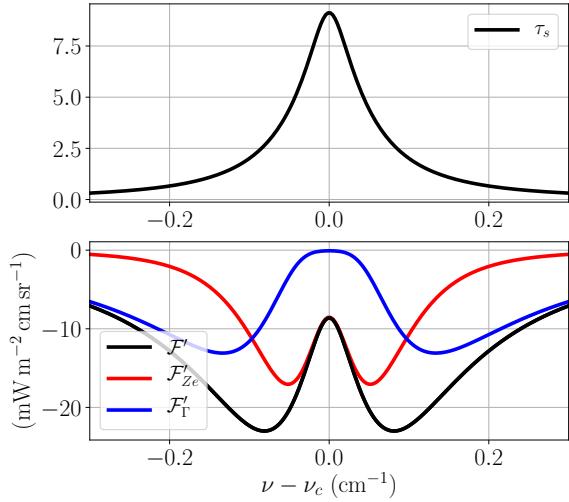


FIG. 8. Same as Fig. 7 except that the intensity of the line is 12 times larger, referred as line of “medium intensity”.

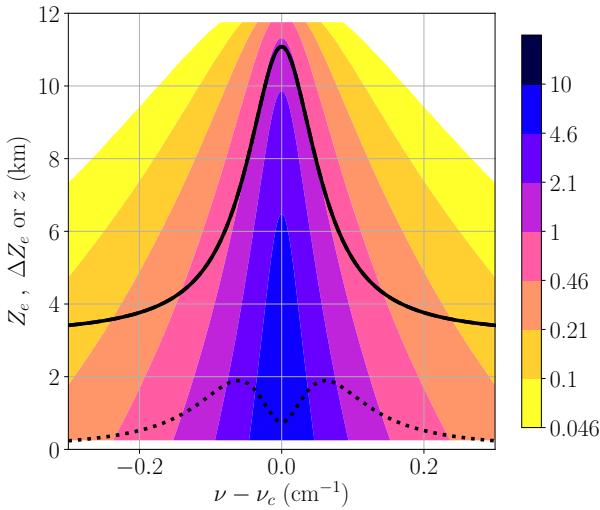


FIG. 9. Emission height Z_e (black continuous line) as a function of the distance from the absorption line center for the same conditions as in Fig. 8, and change ΔZ_e of this emission height when the amount of absorbing gas is doubled (dotted line). Shades indicate the optical thickness τ of the troposphere at altitude z and wavenumber ν .

the mid latitude summer (MLS) atmospheric profile (McClatchey et al., 1972; Anderson et al., 1986) that has often been used to benchmark radiative codes (Ellingson et al., 1991; Collins et al., 2006; Pincus et al., 2015).

As in the previous section, we consider an atmosphere that ends at the tropopause. The temperature and the pressure at the surface and at the tropopause are close to the previous idealized profile ($P_s = 1013\text{ hPa}$, $H_s = 0\text{ m}$, $T_s = 294\text{ K}$, $P_t = 190\text{ hPa}$, $H_t \approx 12.6\text{ km}$, $T_t = 218.4\text{ K}$). The vertical profile of temperature is almost linear with altitude

and therefore the vertical profile of the Planck function at $\nu_c = 550\text{ cm}^{-1}$ is not linear with pressure anymore. The volumetric mass density varies according to the perfect gas law and the atmosphere is discretized into 65 vertical layers. The CO₂ concentration is 287 ppmv as in Collins et al. (2006). We perform the same computations as in the previous section with this new profile, and the results show little differences compared to those displayed on Figures 3 to 6 (not shown). The exact values are slightly modified but all the key features are identical.

a. Single absorption line

We now consider a narrow frequency range around the center of an absorption line instead of a given frequency. Molecules in gases have discrete energy levels and absorption of photons correspond to transitions between these discrete energy levels. The absorption lines are very numerous (many millions) and not infinitely sharp due to broadening mechanisms. In the Earth troposphere, pressure broadening (also named collision broadening) is the dominant effect and will be the only one considered in a first step. In the vicinity of a line center, the spectral absorption coefficient k varies with frequency according to a Lorentzian profile:

$$k = \frac{S}{\pi} \frac{\alpha}{(\nu - \nu_c)^2 + \alpha^2} \quad (15)$$

where S is the line absorption integrated intensity, ν is the wavenumber, ν_c the wavenumber of the line center and α is the half-width at half-height. Lorentz half width is assumed be proportional to $PT^{-0.5}$

$$\alpha(P, T) = \alpha_0 \frac{P}{P_0} \left(\frac{T_0}{T} \right)^{0.5} \quad (16)$$

with $\alpha_0 \approx 0.1\text{ cm}^{-1}$ at $P_0 = 1013\text{ hPa}$ and $T_0 = 300\text{ K}$, which are typical values for the CO₂ lines around 550 cm^{-1} . We assume that the line intensity is constant along the vertical and is multiplied by a factor $f = 1$ to allow a proportional change in absorption within the whole atmosphere, as in previous section.

The sensitivity of the spectral radiance at the tropopause to a fractional change in the absorbing gas for a line can be deduced from single frequency results (Fig. 4). A first example is shown for a single and weak absorption line (Fig. 7). The optical thickness at the absorption line center is about 0.75 and decreases rapidly away from the line center. The sensitivity of the radiance is maximum at the line center and is primarily due to the change in absorptivity (F'_T , blue line) as the optical thickness is small.

This picture is very different for a line whose absorption intensity is 12 times larger and that will be referred later as a line of “medium intensity” (Fig. 8). Around the absorption line center, the sensitivity F'_T due to a change in absorptivity is zero as one may expect from Fig. 4. In

this spectral region the sensitivity \mathcal{F}'_{Z_e} due to a change in emission height is the dominant factor. Close to the absorption line center, the optical thickness is large and the mean emission height is located close to the tropopause (Fig. 9). An increase of optical thickness has little impact on the emission height. Away from the absorption line center, the sensitivity due to a change in emission height is still the dominant factor and an increase of absorbing gas decreases the radiance at the tropopause and therefore increases the greenhouse effect. Further away from the absorption line center, the sensitivity due to a change in total absorption dominates, and slowly decreases away from the absorption line center.

b. Change in emission height when doubling the amount of absorbing gas

As a benchmark the amount of absorbing gas is doubled over the whole atmospheric profile. For the idealized atmosphere, the change ΔZ_e in emission height is zero when the optical thickness τ_s of the tropopause is zero, as one may expect (Fig. 6, dotted line). It increases with τ_s up to more than 2 km for $\tau_s \approx 4$, and then decreases with increasing τ_s as the emission height is already close to the tropopause.

For the weak absorption line, the change in emission height is small. It varies from about 20 meters at 0.3 cm^{-1} from the absorption line center to about 800 meters at the absorption line center (not shown). For the absorption line of medium intensity (Fig. 9), the change in emission height increases from about 200 meters at 0.3 cm^{-1} from the absorption line center up to 2 km at a wave number for which the optical thickness is about 4 and finally decreases to 750 meters at the absorption line center.

From these results, one may expect that for a doubling of the CO_2 concentration, the change in emission height will have a value varying from a few tens of meters in spectral regions where the absorptivity is either very weak or very strong, to a maximum value of $\approx 1 - 2\text{km}$ in spectral regions where the optical thickness is about a few units ($\tau_s \approx 2 - 8$).

The results presented until now can be easily reproduced and provide the basis to understand the key phenomena that drives the greenhouse effect. In the next section we will use this understanding to interpret results produced by a comprehensive reference radiation code.

4. Radiative flux over the whole infrared domain with realistic radiative and thermodynamic properties

Until now we considered only radiances that allowed us to avoid angular integration. In this section we show how the framework based on radiances can be easily transposed to a framework for irradiance, or radiative flux. We use the classical approximations for pristine atmospheres. The atmosphere is absorbing and non-scattering, perfectly

stratified along the horizontal (plane parallel assumption) and the surface has an emissivity of one.

a. Framework for radiative flux

With the above assumptions, the spectral flux F at the tropopause is (Pierrehumbert, 2010; Dufresne et al., 2005):

$$F = \hat{\mathcal{T}}_s B_s + \int_{P_t}^{P_s} \frac{\partial \hat{\mathcal{T}}(P)}{\partial P} B(P) dP \quad (17)$$

where $B = \pi \mathcal{B}$ and $\hat{\mathcal{T}}(P)$ is the spectral hemispherical transmissivity between the pressure level P and the pressure at the tropopause level P_t :

$$\hat{\mathcal{T}}(P) = 2 \int_0^1 \exp(-\tau(P, \mu)) \mu d\mu \quad (18)$$

where $\tau(P, \mu)$ is the spectral directional optical thickness between the tropopause and the pressure level P

$$\tau(P, \mu) = \left| \int_{P_t}^P \frac{f k(P)}{g \mu} dP \right|, \quad (19)$$

where μ is the cosine of the zenith angle, $k(P)$ the specific absorption coefficient at level of pressure P , and $f = 1$ a multiplicative factor as in the previous sections. Equation 17 is similar to Eq. 6 previously used, except that the radiances (\mathcal{F}, \mathcal{B}) have been replaced by the irradiance (or flux) (F, B), and the directional transmissivity \mathcal{T} has been replaced by the hemispherical transmissivity $\hat{\mathcal{T}}$. With these replacements, one can show that equations 8 to 14 can be directly adapted to fluxes. For instance, Eq. 17 can be rewritten as:

$$F = \hat{\mathcal{T}}_s B_s + (1 - \hat{\mathcal{T}}_s) B_e \quad (20a)$$

$$B_e = \int_{P_t}^{P_s} B(P) \omega(P) dP \quad (20b)$$

$$\omega(P) = \frac{1}{1 - \hat{\mathcal{T}}_s} \frac{\partial \hat{\mathcal{T}}(P)}{\partial P} \quad (20c)$$

which can be compared to Eqs. 8a-8c. In Eq. 20a, $\hat{\mathcal{T}}_s B_s$ is termed the surface transmitted irradiance in Costa and Shine (2012). Applying the same replacements to Eqs. 10a-10c allows to split the sensitivity of the flux at the tropopause F' in a contribution $F'_{\hat{\mathcal{T}}}$ due to the change in absorptivity and a contribution F'_{Z_e} due to the change in emission height.

Many radiative codes do not compute the sensitivity F' directly, and a difference in radiances can therefore be more suitable. For two atmospheres $i = 1, 2$ that only differ by the amount of absorbing gases, the flux at the tropopause reads:

$$F_i = \hat{\mathcal{T}}_{s,i} B_s + (1 - \hat{\mathcal{T}}_{s,i}) B_{e,i} \quad (21)$$

One can show (see Sect. A2 in appendix) that the difference between the two fluxes $\Delta F = F_2 - F_1$ reads as:

$$\Delta F = \Delta F_{\hat{\mathcal{T}}} + \Delta F_{Ze} \quad (22a)$$

$$\Delta F_{\hat{\mathcal{T}}} = \left(\hat{\mathcal{T}}_{s,2} - \hat{\mathcal{T}}_{s,1} \right) [B_s - B_{e,1}] \quad (22b)$$

$$\Delta F_{Ze} = (1 - \hat{\mathcal{T}}_{s,2}) [B_{e,2} - B_{e,1}] \quad (22c)$$

$\Delta F_{\hat{\mathcal{T}}}$ quantifies the effect of the change in absorptivity and ΔF_{Ze} the effect of the change in emission height. If F , B_s and $\hat{\mathcal{T}}_s$ are known, $B_{e,2}$ and $B_{e,1}$ can be computed using Eq. 21, and therefore Eqs. 22b and 22c can be used to compute $\Delta F_{\hat{\mathcal{T}}}$ and ΔF_{Ze} . Therefore, any radiative code, no matter how complex, that computes F , B_s and $\hat{\mathcal{T}}_s$, which is generally the case, can be used to compute the changes $\Delta F_{\hat{\mathcal{T}}}$ of the flux at the tropopause that is due to the change in absorptivity and the change ΔF_{Ze} that is due to the change in emission height. However, the change in emission height itself is more difficult to compute as it requires the use of Eq. 14, which is not straightforward for many radiative codes. This is one of the reasons why we used a radiative code based on the Net Exchange Formulation (NEF) (Green, 1967; Cherkaoui et al., 1996; Dufresne et al., 2005)

b. A reference line by line model based on a Net Exchange Formulation

The line by line radiative model we use is presented in Eymet et al. (2016) and its main originality is to rely on the Net Exchange Formalism (NEF). In a first step (Kspectrum code), a synthetic high-resolution (typically 0.0005cm^{-1}) absorption spectra is computed for the required atmospheric profile using the HITRAN 2012 molecular spectroscopic database (Rothman et al., 2013) with Voigt line profiles. For CO₂, sub-lorentzian corrections are taken into account. For H₂O, the CKD continuum is used with a 25cm^{-1} truncation and removing the “base” of each transition (Clough et al., 1989; Mlawer et al., 2012). In a second step (HR_PPart code), radiative transfer is computed based on 1D (over a single line of sight) or 3D (angularly integrated) analytical expressions of spectral radiative Net Exchange Rates and spectral radiative fluxes. We compute the radiative forcing for CO₂ and H₂O changes based on the experiments defined in Collins et al. (2006): the reference experiment, which is the mid latitude summer (MLS) atmospheric profile with a CO₂ concentration of 287ppmv (called 1a), an experiment where the CO₂ concentration is doubled (called 2b), and an experiment where the CO₂ concentration is doubled and the concentration of H₂O is increased by 20% (called 4a). In this example, the only absorbing gases considered are H₂O, CO₂ and ozone and the troposphere is discretized into 31 vertical layers. The results compare well

with those published by Collins et al. (2006), as shown on Table 1.

c. Results for a realistic atmospheric profile

We use the same mid latitude summer atmospheric profile and consider only the troposphere, from the surface ($P_s = 1013\text{hPa}$, $H_s = 0\text{m}$, $T_s = 294\text{K}$) to the tropopause ($P_t = 190\text{hPa}$, $H_t \approx 12.6\text{km}$, $T_t = 218.4\text{K}$), as presented above.

We first focus on two CO₂ weak absorbing lines. In Fig. 10, and only in this figure, we exclude absorption by the H₂O continuum in order to have an optical thickness that is as small as possible. For the weaker absorption line for which the optical thickness is always less than one (Fig. 10, left column), the shape of the optical thickness resembles that of the idealized one (Fig. 7). The optical thickness is low ($\tau_s \ll 1$) and the emission height is about 2-3 km, as expected from Fig. 9. When doubling the CO₂ concentration, the change in optical thickness is almost equal to the value for the reference atmosphere, the difference is due to some absorption by H₂O. The change in emission height is less than 100m at wavenumbers far away from the absorption line center and increases to a few hundred meters at the absorption line center. The change in the tropopause irradiance is largely dominated by the contribution of the change in absorptivity.

For a more absorbing line with a companion weak absorbing line (Fig. 10, right column), the emission height is about 2-3 km far from the absorption line center, where the optical thickness is below one. At the absorption line center, the emission height reaches 8 km, which is closer to the tropopause. When doubling the CO₂ concentration, the change in emission height is a few hundred meters far from the absorption line center to more than a kilometer at the absorption line center. The change in the tropopause irradiance is dominated by the contribution of the change in emission height.

The results we obtained with the various idealized configurations are consistent with those we obtained with the reference model. The understanding we gained with the idealized examples can be applied to interpret the results with much more complex and realistic models.

We now consider the “thermal infrared” spectral interval from 100 to 2500 cm^{-1} (4 to $100\text{ }\mu\text{m}$). On Fig. 11, 12 and 14, variables are smoothed on a 10cm^{-1} spectral interval to make the figure more readable. The spectral dependency of the radiative flux at the TOA, at the tropopause, within the atmosphere, and of the radiative cooling rate in the atmosphere, as well as how they change when changing the CO₂ concentration have already been addressed in many studies (Kiehl and Ramanathan, 1983; Kiehl, 1983; Charlock, 1984; Clough and Iacono, 1995; Harries et al., 2001; Huang, 2013). Mlynaczak et al. (2016) show that

experiments	$\Delta\bar{F}$ TOA		$\Delta\bar{F}(200)$		$\Delta\bar{F}_s$	
	KS	C06	KS	C06	KS	C06
2 \times CO ₂ (2b-1a)	2.81	2.80 \pm 0.06	5.57	5.48 \pm 0.07	1.67	1.64 \pm 0.04
1.2 \times H ₂ O (4a-2b)	3.71	3.78 \pm 0.1	4.60	4.57 \pm 0.14	11.43	11.52 \pm 0.40

TABLE 1. Difference of the net flux (in Wm⁻²) at the TOA, at 200 hPa ($\Delta\bar{F}(200)$) and at the surface ($\Delta\bar{F}_s$) for a CO₂ doubling and for an increase of H₂O by 20% for the MLS atmospheric profile and for the thermal infrared spectral interval (100-2500 cm⁻¹, i.e. 4 to 100 μ m). The results computed with our model (KS) are compared to those published by Collins et al. (2006) (C06) for an ensemble of line by line models using the same atmospheric profiles (see Sect. 4-b)

these results were remarkably insensitive to known uncertainties in the main CO₂ spectroscopic parameters. Zhong and Haigh (2013) showed how the flux at the TOA varies over a wide range of CO₂ values, and they showed that the spectral response is very different depending on the CO₂ concentration. Here we consider the response for an atmosphere with a CO₂ concentration close to its preindustrial value (287ppmv).

The total optical thickness τ_s (Fig. 11-a, black line) is primarily due to H₂O absorption, except around 660 and 2300 cm⁻¹ where the two CO₂ strong absorption band systems at 15 μ m and 4.3 μ m (magenta) are dominant. The total optical thickness varies over many orders of magnitude, from about one in the atmospheric window (between 800 and 1200 cm⁻¹) to $10^4 - 10^5$ in the H₂O and CO₂ absorption bands. When the data is not smoothed, the range is even larger, from a few tenths up to 10^6 .

The emission height (Fig. 11-b) almost increases with the logarithm of the total optical thickness τ_s (Huang and Bani Shahabadi, 2014). It varies for 2km in the atmospheric window up to 12km, i.e. almost the tropopause height, in spectral region where the optical thickness is very high, especially for the CO₂ bands. For the same optical thickness, the emission height in the CO₂ absorption bands are larger than for the H₂O absorption bands as the CO₂ concentration is uniform over the whole troposphere whereas the H₂O concentration strongly decreases with height.

We define the emission temperature as the temperature for which the Planck function is equal to B_e defined by Eq. 20b. The emission temperature (Fig. 11-c) directly follows the evolution of the emission height. The dependence is about 7K/km, as one may expect from the value of the temperature gradient in the troposphere. The upward flux at the tropopause may have been emitted either from the surface or from the troposphere (Eq. 17 and 6). One can see in Fig. 11-d that almost all the flux at the tropopause has been emitted by the troposphere, except in the atmospheric window where both the emission by the surface and the troposphere contribute almost equally (Costa and Shine, 2012).

The ozone absorption band around 1050cm⁻¹ has a specific signature as ozone is mainly located in the higher part of the troposphere. This band has little impact on the optical thickness but has a visible signature on the emission

height, the emission temperature, and the outgoing flux (Fig. 11).

Fig. 12 displays the changes in total optical thickness, emission height, emission temperature and upward flux at the tropopause when doubling the CO₂ concentration or when increasing the H₂O concentration by 20%. For the CO₂ 15 μ m band system (660cm⁻¹), the change in emission height, emission temperature, and tropopause flux is maximum on the edges of the band (Fig. 12-bcd), where the CO₂ optical thickness is about a few units (Fig. 11-a). In these spectral regions, the change in emission height is about 1km and the change in emission temperature is about 7K. The change in emission height is almost zero at the band center as the emission height is already close to the tropopause, i.e., close to the maximum height. The change in the flux at the tropopause is almost only due to the change in emission height (Fig. 12-d). For the 4.3 μ m (2300 cm⁻¹) CO₂ band, the changes in emission height and emission temperature resemble those for the 15 μ m (660cm⁻¹) band, but these changes have almost no impact on the tropopause flux as the Planck function is almost zero at these wave numbers for the atmospheric temperature. In addition to these two very strong absorption bands, CO₂ also has some minor bands that produce small changes in emission height, emission temperature and tropopause flux. In the spectral domain of these minor bands, the optical thickness is small (about 10^{-1}) and is due to absorption by both H₂O and CO₂. As a result, both the change in emission height and in absorptivity play a comparable role, whereas the change in absorptivity would have had a dominant role if CO₂ were the only absorbing gas. Note that this holds for the current atmosphere but not for an atmosphere with very high CO₂ concentration: these “minor” bands contribute to the CO₂ forcing by about 6% in current conditions, but they contribute by about 25% for CO₂ concentration that are 100 times larger (Augustsson and Ramanathan, 1977; Zhong and Haigh, 2013).

As the change ΔZ_e in emission height strongly varies with wavenumber, we define its average value in two ways. The first is the broadband average $\langle \Delta Z_e \rangle_P$, where ΔZ_e is weighted by the Planck function at surface temperature, as for the broadband absorptivity shown on Fig. 1-a. We found a value of 150m, exactly as Held and Soden (2000). As explained in this article, the broadband change

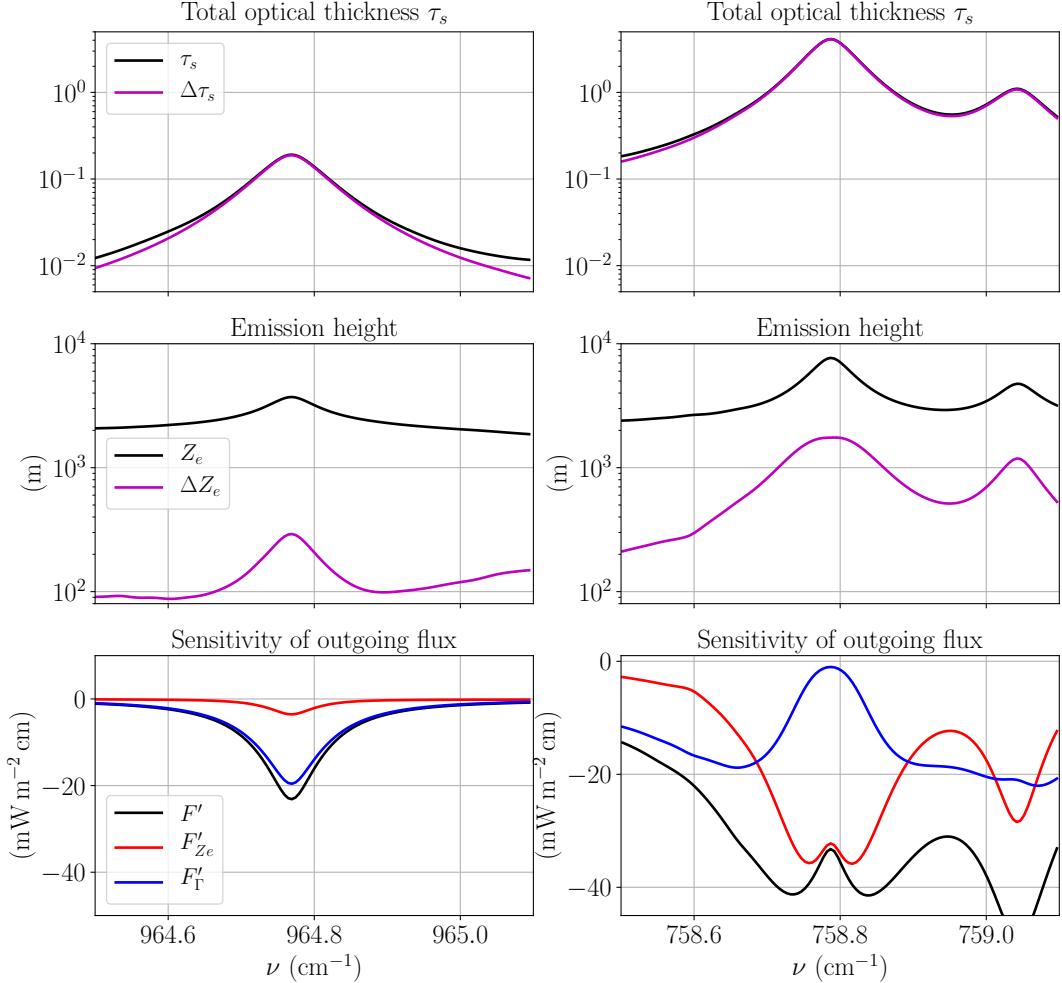


FIG. 10. Total optical thickness τ_s of the troposphere (black line) and its change $\Delta\tau_s$ (magenta line) for a CO₂ doubling (top row), emission height Z_e (black line) and its change ΔZ_e (magenta line) for a CO₂ doubling (middle row), and sensitivity F' of the flux at the tropopause (black line) to a fractional change in CO₂ and contributions of change in absorptivity (blue line: F'_Γ) and in emission height (red line: F'_{Z_e}) (bottom row) as a function of wave-number (cm $^{-1}$). The figure shows a weak absorption line (left column: 964.5–965.1 cm $^{-1}$) and an intermediate absorption line with a companion weak absorbing line (right column: 758.5–759.1 cm $^{-1}$).

in emission height can be directly used to compute the radiative forcing. However, the change in the flux at the tropopause is different from zero only in limited spectral regions where ΔZ_e is also large (Fig. 12). Therefore we define a second average, $\langle \Delta Z_e \rangle_F$, namely the “forcing average” change in emission height defined as the average of ΔZ_e weighted by ΔF_{Z_e} :

$$\langle \Delta Z_e \rangle_F = \frac{\int_0^\infty \Delta Z_e(\nu) \Delta F_{Z_e}(\nu) d\nu}{\int_0^\infty \Delta F_{Z_e}(\nu) d\nu} \quad (23)$$

This quantity is the change in emission height that actually contributes to the radiative forcing. We obtain a value of 1025 m, which is much larger than the broadband mean. The change in CO₂ concentration impacts the flux at the tropopause in the very few spectral regions where the optical thickness of the atmosphere is about a few units. In these spectral regions the change in emission height is on average 1025 m. The mean emission height itself is less sensitive to the average method: The broadband emission

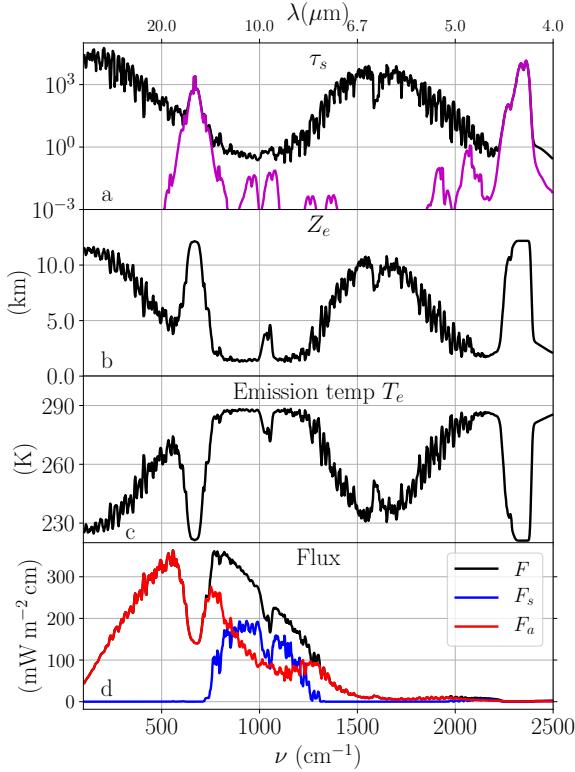


FIG. 11. (a) Optical thickness τ_s (black line; total optical thickness; magenta line: optical thickness due to CO_2), (b) emission height Z_e , (c) emission temperature T_e , and (d) upward radiative flux at the tropopause (black: total, F ; blue: emitted by the surface, F_s ; red: emitted by the troposphere, F_a) for the MLS atmospheric profile. The abscissa is given in wave-number (cm^{-1}) at the bottom and in wavelength (μm) at the top. Variables are smoothed on a 10cm^{-1} spectral interval.

height is 5800m whereas the “forcing average” emission height is 6100m.

When the H_2O concentration is increased, the change in emission height is about 200 m (Fig. 12-b) over spectral intervals that are much wider ($100\text{-}600\text{cm}^{-1}$, $1300\text{-}2000\text{cm}^{-1}$) than for CO_2 . In these intervals the absorption by H_2O is strong and the change of the flux at the tropopause is almost only due to the change in emission height (Fig. 12-e). In spectral regions where absorption by CO_2 dominates ($600\text{-}750\text{cm}^{-1}$), the change in H_2O is completely masked by the CO_2 absorption. In most of the atmospheric window ($750\text{-}1300\text{cm}^{-1}$), the change in emission height is small ($< 100\text{m}$) and the change of the flux at the tropopause is mainly due to the change in absorptivity, with a significant contribution of the water vapor continuum (Costa and Shine, 2012). An exception is around 1050 cm^{-1} where ozone absorbs. In this spectral region both the ozone and the water vapor emit radiation

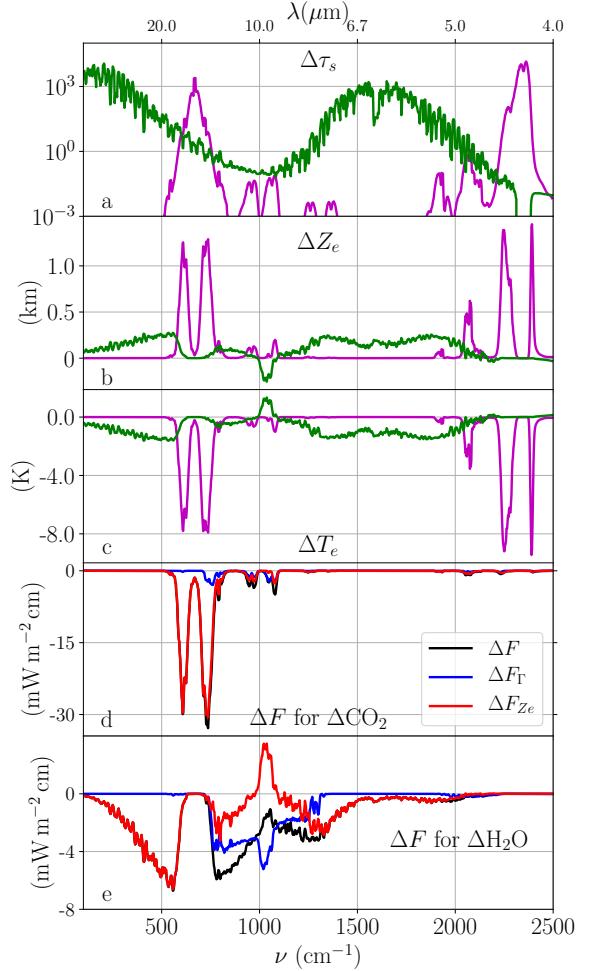


FIG. 12. Changes due to a CO_2 doubling (magenta line) and to an increase by 20% of the H_2O concentration (green line) of the optical thickness τ_s (a), of the emission height Z_e (b), and of the emission temperature T_e (c) for the same atmospheric profile as in Fig. 11. The changes ΔF of the flux at the tropopause (black line) and the contributions of the change in atmospheric absorptivity (blue line, ΔF_{Fr}) and in emission height (red line, ΔF_{Z_e}) are shown on (d) for CO_2 and on (e) for H_2O . The abscissa is given in wave-number (cm^{-1}) at the bottom and in wavelength (μm) at the top. Variables are smoothed on a 10cm^{-1} spectral interval.

and the emission height includes both the contribution of ozone, which is mainly located in the high troposphere, and the contribution of water vapor, which is mainly located in the lower troposphere. When the H_2O concentration increases, the radiation emitted by H_2O that reaches the tropopause increases whereas the radiation emitted by ozone that reaches the tropopause does not change. As

atm. profile	experiments	$\Delta\bar{F}$ (Wm ⁻²)	$\Delta\bar{F}_{Ze}$ (Wm ⁻²)	$\Delta\bar{F}_{\hat{\gamma}}$ (Wm ⁻²)	$\Delta\bar{F}_{Ze}/\Delta\bar{F}$ (-)	$\Delta\bar{F}_{\hat{\gamma}}/\Delta\bar{F}$ (-)	$\Delta\hat{\mathcal{T}}_s$ (-)
MLS	2×CO ₂ (2b-1a)	-3.83	-3.46	-0.37	0.90	0.10	$-4.1 \cdot 10^{-3}$
	1.2×H ₂ O (4a-2b)	-3.78	-2.21	-1.57	0.58	0.42	$-2.7 \cdot 10^{-2}$

TABLE 2. Difference $\Delta\bar{F}$ of the upward flux at the tropopause, difference $\Delta\bar{F}_{Ze}$ of this flux due to change in emission height, difference $\Delta\bar{F}_{\hat{\gamma}}$ due to change in absorptivity, relative contribution of each of the changes ($\Delta\bar{F}_{Ze}$ and $\Delta\bar{F}_{\hat{\gamma}}$) to the total $\Delta\bar{F}$, and change $\Delta\hat{\mathcal{T}}_s$ of the broadband transmissivity of the atmosphere. The differences are computed for a CO₂ doubling (2b-1a, first row) and an increase of H₂O by 20% (4a-2b, second row), for the atmospheric profiles presented in the text (Sect. 4-b).

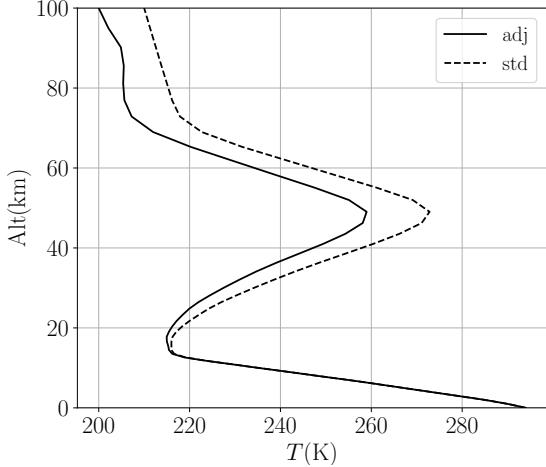


FIG. 13. Temperature as a function of altitude for the full MLS atmospheric profile, i.e. including the stratosphere. Both the reference temperature (dash line) and the temperature after the stratosphere has adjusted to a doubling of the CO₂ concentration (continuous line) are shown.

a result the emission height decreases by about 200m (Fig. 12-b), the emission temperature increases (Fig. 12-c) and the contribution of the change in emission height to the flux at the tropopause is positive (Fig. 12-e).

When considering the radiative flux over the whole thermal infrared domain, the decrease of the flux at the tropopause due to an increase of CO₂ is primarily due (by about 90%, Table 2) to the change in emission height, the change in absorptivity playing a minor role (about 10%). For an increase of water vapor, the change in absorptivity plays a more important role (about 40%) but the change in emission height still plays the dominant role ($\approx 60\%$). However, this significant contribution of the change in absorptivity for H₂O is primarily due to the H₂O continuum. When the continuum is suppressed, the change in emission height is as high as 80% and the contribution of the change in absorptivity reduces to 20%.

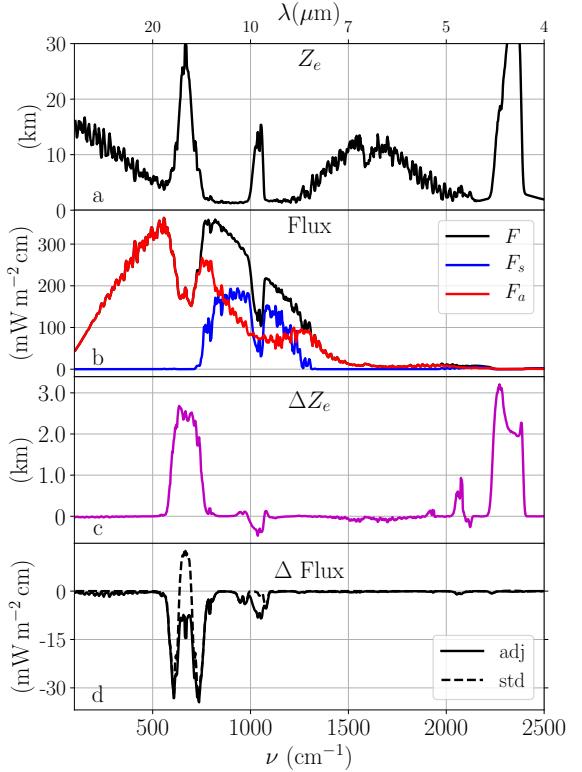


FIG. 14. For the MLS atmospheric profile including the stratosphere, emission height Z_e (a), radiative flux at the TOA (b) total (black), emitted by the surface (blue) and emitted by the atmosphere (red). Change in emission height (c) (ΔZ_e , magenta) and in the flux at the TOA (d) if the temperature in the stratosphere is held fixed (dash line) or is adjusted (continue line). The abscissa is given in wave-number (cm⁻¹) at the bottom and in wavelength (μm) at the top. Variables are smoothed on a 10cm⁻¹ spectral interval.

d. Including the stratosphere

So far and for simplicity we considered an atmosphere that extends from the surface to the tropopause, and therefore in which the vertical temperature gradient is always negative and driven by the convective adjustment. We now consider an atmosphere that extends to an altitude

of 100 km and will show that the main results are still valid when the temperature adjustment of the stratosphere is taken into account.

In the stratosphere, the radiative cooling is compensated by the dynamic heating with a relaxation time of a few months. As the dynamics in the troposphere and in the stratosphere are weakly coupled, it has been shown (Hansen et al., 1981, 1997; Stuber et al., 2001; Forster et al., 2007) that it is more relevant to compute the radiative forcing after allowing stratospheric temperatures to adjust to a new radiative equilibrium than to compute the radiative forcing with a fixed stratospheric temperature. The stratospheric temperature adjustment is computed assuming no change in stratospheric dynamics as follows: after computing the radiative budget $S_1(z)$ at each altitude z for the reference concentration and temperature, the radiative budget $S_2(z)$ at each altitude z is computed with the same temperature profile but a modified CO₂ concentration. The temperature in the stratosphere is then adjusted until $S_2(z) \approx S_1(z)$ at each altitude z of the stratosphere. The results we obtain for the MLS profile and a doubling of the CO₂ concentration are shown in Fig. 13. By construction the temperature in the troposphere does not change. The temperature in the stratosphere decreases as expected (Hansen et al., 1997; Stuber et al., 2001), with a temperature cooling of 5 to 10K.

Compared to the troposphere only case (Fig. 11), including the stratosphere increases the emission height in the center of the CO₂ absorption band systems at 15 and 4.3μm where the emission height reaches values up to 30 to 40km (Fig. 14-a). This height is even larger when looking at the full resolution data (not shown). Including the stratosphere increases the optical thickness around the 9.7 μm ($\approx 1050\text{cm}^{-1}$) O₃ absorption band by a few units, which has a significant impact on both the emission height and the flux at the TOA (Fig. 14-a and b).

When doubling the CO₂ concentration, the change in emission height (Fig. 14-c) is comparable to the case without stratosphere (Fig. 12-b) except in the 15 and 4.3μm CO₂ absorption bands. At these band centers, the emission height can now be larger than the tropopause height, the increase in emission height is not blocked anymore and it has an almost constant value of about 3 km. One can show that the change in emission height is almost constant for a well-mixed absorption gas when absorption is saturated because the emission height is then close to the height where the optical thickness is equal to one (Fig. 6). This large change in emission height has a clear signature on the change of the flux at the TOA for the 15μm CO₂ absorption band. At the absorption band center, a higher emission height leads to an increase of the outgoing flux because the temperature vertical gradient in the stratosphere is positive. However, this happens only if the temperature in the stratosphere is fixed

(Fig. 14-d, dash line) as already shown (Kiehl, 1983; Charlock, 1984). If the temperature of the stratosphere is adjusted as explained above, the decrease of temperature in the stratosphere leads to a decrease of the emitted radiation. As a result, the change in the outgoing flux at the center of the 15μm CO₂ absorption band is slightly negative. The pattern of the change of the spectral flux around the 15μm CO₂ absorption band is similar if the atmosphere only extends up to the tropopause (Fig. 12-d) and if the atmosphere extends higher than the tropopause but the stratospheric adjustment is considered (Fig. 14-d, continuous line). At the first order, the interpretation of the results we obtained with an atmosphere reduced to the troposphere can be extended to a full atmosphere where the temperature of the stratosphere is adjusted. However, the adjustment of the stratosphere also impacts the emission by other gases: H₂O for wavenumbers lower than 500cm⁻¹ and ozone near 1050cm⁻¹.

5. Summary and conclusion

In this article we presented a framework that allows us to make a direct and precise link between the basic radiative transfer equations in the atmosphere on one hand, and the concept of emission height on the other hand. This allowed us to quantify how much a change in the greenhouse effect originates from a change in the emission height and how much originates from a change in the absorptivity of the atmosphere, i.e. the absorption over the entire height of the atmosphere.

The fact that a saturation of the absorptivity of the atmosphere leads to a saturation of the greenhouse effect is directly related to the hypothesis of an isothermal atmosphere. When this simplification is removed and the decrease of temperature with altitude is considered, as it is the case in the troposphere, the greenhouse effect can continue to increase even if the absorptivity of the atmosphere is saturated.

The fundamental difference between our approach and other approaches such as the “bulk emission temperature” (Benestad, 2017) or the “brightness temperature” commonly used in remote sensing, is that we split the radiation leaving the atmosphere toward space in two terms: the radiation that has been emitted by the surface (termed surface transmitted irradiance in Costa and Shine (2012)), and the radiation that has been emitted by the atmosphere. The fraction between these two terms is directly driven by the absorptivity of the atmosphere (Eq. 8a). When the absorptivity is zero, the total flux leaving the atmosphere originates from radiation emitted by the surface, and the atmosphere has no radiative impact. When the absorptivity is close to 1, i.e. when the total optical thickness of the atmosphere is larger than about 4, the opposite situation happens: the total flux leaving the atmosphere has been emitted by the atmosphere, the surface does not have

any direct radiative impact on the flux leaving the atmosphere, and increasing the optical thickness does not have any influence on the ratio between these two terms anymore. However, this does not mean that the greenhouse effect does not change. Increasing the optical thickness increases the mean emission height and if the atmosphere is not isothermal, a change in emission height translates in a change in outgoing radiative flux.

For an increase in CO₂ concentration above its preindustrial value, the increase of the greenhouse effect is primarily due (by about 90%) to the change in emission height. In spectral regions that actually contribute to the radiative forcing, the increase in emission height is about 1 km for a doubling of the CO₂ concentration. As the mean emission height is about 6km, i.e. above where most of the mass of water vapor is located, the radiative effect of this change of emission height is weakly affected by the water vapor amount. This explain why the increase of the greenhouse effect when increasing CO₂ is weakly dependent of the H₂O amount (Fig. 1-b), in contrast with the broadband absorptivity. The change in emission height will be of comparable magnitude for any other well mixed absorbing gases in the spectral domains where the absorptivity is saturated. For an increase of water vapor, the change in absorptivity plays a more important role (about 40%) but the change in emission height is still about 60%. Indeed, away from the atmospheric window, the absorptivity by water vapor becomes saturated and the change in emission height becomes therefore dominant.

The emission height depends on both the temperature profile and the optical properties (Eqs. 14 and 11). We showed that the classical assumption that the emission height is close to the altitude where the optical thickness between this altitude and the top of the atmosphere is equal to one is valid only for atmospheres that are optically thick enough ($\tau_s > 4$). For optically thin atmospheres or with optical thickness close to one, this assumption is not valid and leads to an underestimation of the emission height.

Considering the real temperature vertical profile in the whole atmosphere makes simplified analysis of the greenhouse effect a priori difficult. However, this complexity is essentially eliminated when considering the adjustment of the stratospheric temperature. This had long been shown when considering global fluxes. Here, we have shown that this is also the case when looking at the change in spectral fluxes and emission altitude, and therefore that it is legitimate to replace the vertical profile of the entire atmosphere by the vertical profile of the troposphere alone, for simplified thinking.

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APPENDIX

A1. Analytical expression for the idealized atmosphere

In this section we take advantage of the assumption of the idealized atmosphere (section 2) and in particular that the spectral Planck function increases linearly with pressure (Eq. 4).

a. Outgoing radiance \mathcal{F} at the tropopause

For the idealized atmosphere, Eq. 8b can be integrated analytically and one obtains (after an integration by parts):

$$\mathcal{B}_e = \mathcal{B}(P_s) + [\mathcal{B}(P_t) - \mathcal{B}(P_s)] \left[\frac{1}{1 - e^{-\tau_s}} - \frac{1}{\tau_s} \right] \quad (\text{A1})$$

The outgoing radiance \mathcal{F} at the tropopause is (Eq. 6):

$$\mathcal{F} = \mathcal{B}_s e^{-\tau_s} + (1 - e^{-\tau_s}) \mathcal{B}_e \quad (\text{A2})$$

If the atmosphere is optically very thin ($\tau_s \ll 1$), one may obtain¹ that $\mathcal{B}_e \approx [\mathcal{B}(P_t) + \mathcal{B}(P_s)]/2$ and therefore $\mathcal{F} \approx \mathcal{B}_s + \tau_s [\mathcal{B}_e - \mathcal{B}_s]$. The outgoing radiance is the same for the isothermal and non-isothermal atmosphere, it is equal to the radiance \mathcal{B}_s emitted by the surface when the atmosphere is perfectly transparent ($\tau_s = 0$), and then decreases linearly with τ_s when the latter increases. In contrast, if the atmosphere is optically very thick ($\tau_s \gg 1$), $\mathcal{F} \approx \mathcal{B}_e \approx \mathcal{B}(P_t)$, the outgoing radiance is equal to the radiance emitted by a black-body, which temperature is that at the tropopause.

b. Weight $\omega(P)$

$\omega(P)$ is the normalized weighting function to compute the equivalent blackbody emission of the atmosphere (Eq. 8b). Note that according to Eq. 8c, $\int_{P_t}^{P_s} \omega(P) dP = 1$, $-\omega(P)$ can be interpreted as a probability density function. For the idealized atmosphere, an according to Eqs. 5, 7 and 8c

$$\omega(P) = \frac{1}{1 - \mathcal{T}_s} \left(\frac{-kf}{g} \right) e^{-kf(P-P_t)/g} \quad (\text{A3})$$

¹a second order Taylor development is required for $1/(1 - e^{-\tau_s})$

If the atmosphere is optically thin, $\tau_s = kf(P_s - P_t)/g \ll 1$, and after a first order Taylor expansion one obtains:

$$\omega(P) \approx \frac{-1}{P_s - P_t} \quad (\text{A4})$$

If the atmosphere is optically thin, the weight ω is constant along the vertical.

If the atmosphere is optically thick, $\tau_s = \kappa(P_s - P_t) \gg 1$, $T_s \approx 0$ and, according to Eq. A3, $\omega \approx 0$ in the lower troposphere, and $\omega \approx \frac{-kf}{g}$ close to the top of the atmosphere.

A2. Difference in TOA flux when changing the atmospheric absorption

The difference of the flux at the TOA for two atmospheres that only differ by their absorbing gases can be written using Eqs 21 and 20b as:

$$\begin{aligned} F_2 - F_1 &= \left(\hat{\mathcal{T}}_{s,2} - \hat{\mathcal{T}}_{s,1} \right) B_s \\ &\quad + (1 - \hat{\mathcal{T}}_{s,2}) \int_{P_t}^{P_s} \omega_2(P) B(P) dP \\ &\quad - (1 - \hat{\mathcal{T}}_{s,1}) \int_{P_t}^{P_s} \omega_1(P) B(P) dP \end{aligned} \quad (\text{A5})$$

which can be written as:

$$\begin{aligned} F_2 - F_1 &= \left(\hat{\mathcal{T}}_{s,2} - \hat{\mathcal{T}}_{s,1} \right) B_s \\ &\quad + (1 - \hat{\mathcal{T}}_{s,2}) \int_{P_t}^{P_s} (\omega_2(P) - \omega_1(P)) B(P) dP \\ &\quad - (\hat{\mathcal{T}}_{s,2} - \hat{\mathcal{T}}_{s,1}) \int_{P_t}^{P_s} \omega_1(P) B(P) dP \end{aligned} \quad (\text{A6})$$

and finally as:

$$\begin{aligned} F_2 - F_1 &= \left(\hat{\mathcal{T}}_{s,2} - \hat{\mathcal{T}}_{s,1} \right) [B_s - B_{e,1}] \\ &\quad + (1 - \hat{\mathcal{T}}_{s,2}) [B_{e,2} - B_{e,1}] \end{aligned} \quad (\text{A7})$$

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